GAYAZA HIGH SCHOOL

S.4 MATH WORKSHEET TWO

ORDER OF OPERATIONS WITH FRACTIONS

(BODMAS)

PREREQUISITE KNOWLEDGE

- LCM OR EQUIVALENT FRACTIONS
- ADDITION AND SUBTRACTION OF FRACTIONS
- MULTIPLICATION AND DIVISION OF FRACTIONS

Order of Operations (BODMAS)

- 1. Do all operations inside parentheses (brackets) and other grouping symbols.
- 2. Evaluate orders e.g. exponents, powers, etc. commonly known as "of"
- 3. Multiply and divide from left to right.
- 4. Add and subtract from left to right.

Example 1

Solve:
$$\frac{1}{3} \times \left(\frac{2}{3}\right)^2 - \frac{1}{9}$$

There are no operations inside parentheses so evaluate the exponents first.

$$=\frac{1}{3}\times\left(\frac{2}{3}\times\frac{2}{3}\right)-\frac{1}{9}$$

$$=\frac{1}{3}\times\frac{4}{9}-\frac{1}{9}$$

Multiply next

$$=\frac{4}{27}-\frac{1}{9}$$

Always multiply before adding or subtracting.

$$LCM = 27$$

$$=\frac{4-3}{27}$$

$$=\frac{1}{27}$$

Now subtract. Remember to get a common denominator when subtracting OR LCM of the denominators.

Example 2

Solve:
$$\frac{3}{5} - \frac{1}{2} \times \frac{1}{3}$$

$$=\frac{3}{5}-\frac{1}{6}$$

$$=\frac{3\times 6-1\times 5}{30}$$

$$=\frac{18-5}{30}$$

$$=\frac{13}{30}$$

Always multiply before adding or subtracting.

LCM of 5 and 6 is 30

Subtracting fractions

Example 3

Solve:
$$\frac{1}{3} \div \frac{7}{5} - \frac{1}{7}$$

Always divide before adding or subtracting.

$$=\frac{1}{3}\times\frac{5}{7}-\frac{1}{7}$$

When dividing, invert and multiply.

$$=\frac{5}{21}-\frac{1}{7}$$

LCM of 21 and 7 is 21

$$=\frac{5-3}{21}$$

Subtracting fractions

$$=\frac{2}{21}$$

Example 4

Solve:
$$\frac{3}{5} + \frac{2}{3} - \left(\frac{1}{5} + \frac{1}{3}\right)$$

Perform operations inside parentheses first.

$$=\frac{3}{5}+\frac{2}{3}-\left(\frac{3+5}{15}\right)$$

LCM of 5 and 3 is 15

$$=\frac{3}{5}+\frac{2}{3}-\frac{8}{15}$$

Now add and subtract from left to right.

$$=\frac{3\times3+2\times5-8\times1}{15}$$

LCM of 5, 3 and 15 is 15

$$=\frac{9+10-8}{15}$$

$$=\frac{19-8}{15}$$

$$=\frac{11}{15}$$

Example 5

Solve:
$$9 \div \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} + \frac{1}{2} - 1$$

Multiply and divide from left to right.

$$=\frac{9}{1}\times\frac{3}{1}\times\frac{1}{3}\times\frac{1}{3}+\frac{1}{2}-1$$

When dividing, invert (reciprocate) and multiply.

$$= \frac{27}{1} \times \frac{1}{3} \times \frac{1}{3} + \frac{1}{2} - 1$$

$$=\frac{27}{3}\times\frac{1}{3}+\frac{1}{2}-1$$

$$=\frac{27}{9}+\frac{1}{2}-1$$

Add and subtract from left to right.

$$=\frac{27}{9}+\frac{1}{2}-\frac{1}{1}$$

LCM of 9 and 2 is 18

$$= \frac{27 \times 2 + 1 \times 9}{18} - \frac{1}{1}$$

$$=\frac{54+9-18}{18}$$

$$=\frac{63-18}{18}$$

$$=\frac{45}{18}$$

$$=2\frac{9}{18}$$

Always simplify your fractions

$$=2\frac{1}{2}$$

Example 4

Solve:

$$=\frac{\frac{3}{5}+\frac{2}{3}}{\frac{1}{4}\times 9\frac{1}{9}}$$

You can first work out the numerator and the denominator separately and then combine them with the division operation.

OR

$$= \left(\frac{3}{5} + \frac{2}{3}\right) \div \left(\frac{1}{4} \times 9\frac{1}{9}\right)$$
$$= \left(\frac{9+10}{15}\right) \div \left(\frac{1}{4} \times \frac{82}{9}\right)$$

$$= \left(\frac{15}{15}\right) \div \left(\frac{1}{2} \times \frac{1}{9}\right)$$

$$=\frac{19}{15}\div\frac{41}{18}$$

$$=\frac{19}{15}\times\frac{18}{41}$$

$$=\frac{19}{5}\times\frac{6}{41}$$

$$=\frac{114}{205}$$

Put numerator in brackets and divide with denominator also in brackets, then follow BODMAS

Adding in the 1^{st} brackets and in reducing 82 and 4 by 2 in the 2^{nd} brackets

Reducing 18 and 15 by 3

Multiply the fractions

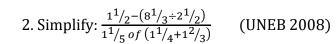
1. Evaluate the following fractions.

(a)
$$1\frac{1}{4} + 2\frac{1}{2} - 1\frac{3}{4}$$

(b)
$$2\frac{1}{2} \times 3\frac{2}{3} \div 1\frac{5}{6}$$

(c)
$$3\frac{1}{5} of \left(2\frac{1}{2} + 7\frac{5}{8}\right)$$

(d)
$$\frac{3^{1}/_{8}+1^{2}/_{3}}{2/_{3}\times^{5}/_{12}}$$





3. Evaluate;
$$\frac{1\frac{1}{5}+4\frac{1}{2}\div1\frac{1}{2}}{3\frac{3}{5}-2\frac{2}{5}\times1\frac{1}{4}}$$

4. Simplify:
$$\frac{\left(3\frac{5}{6} \div 2\frac{2}{15}\right) \times \frac{3}{23}}{5\frac{1}{3} - 2\frac{7}{12}}$$

$$\frac{\frac{1}{2} + \left(\frac{3}{5} \times 1\frac{1}{4}\right)}{1\frac{1}{8} - \frac{3}{4}}$$
 (UNEB 2016)

END.